# Multi-Type Services Coexistence in Uplink NOMA for Dual-Layer LEO Satellite Constellation

Qifan Hu, Jian Jiao, Member, IEEE, Ye Wang, Member, IEEE, Shaohua Wu, Member, IEEE, Rongxing Lu, Fellow, IEEE and Qinyu Zhang, Senior Member, IEEE

Abstract-The upcoming mega low-earth orbit (LEO) highthroughput satellite constellation is regarded as an emerging paradigm shift in the fifth generation-advance (5GA) networks. In this paper, we propose a multi-type services coexistence handover (MSCH) non-orthogonal multiple access (NOMA) scheme for a dual-layer mega LEO satellite constellation, which can simultaneously and efficiently provide uplink NOMA for three types of 5G user equipments (UEs): mission critical communications (MCC) UEs (CUs), massive machine-type communications (mMTC) UEs (MUs) and enhanced mobile broadband (eMBB) UEs (EUs). The EUs are mainly served in the higher layer satellites for longer service duration and may handover to the lower layer satellites to coexist with CUs or MUs. Moreover, the CUs and MUs perform grant-based (GB) and grant-free (GF) NOMA on resource blocks (RBs) in the lower layer satellites, respectively. Then, we derive the closed-form expressions of three specific key performance indicators (KPIs), i.e., outage probability (OP), system throughput (ST), and ergodic capacity (EC) in the MSCH NOMA scheme, and design five corresponding NOMA algorithms. Simulation results verify the accuracy of our theoretical derivations, and show that the proposed NOMA schemes can achieve better KPI performance than the state-of-art ones.

*Index Terms*—Mega LEO HTS constellation, uplink NOMA transmission, multi-layer handover, outage probability, ergodic capacity, system throughput

## I. INTRODUCTION

Non-terrestrial networks (NTN) are expected to foster the roll out of limited terrestrial fifth generation (5G) network in un-served and underserved areas, and enable 5G-advance (5GA) services at *anywhere and anytime* in cost effective manner [1]. Recently, several giant low earth orbit (LEO) high-throughput satellite (HTS) constellations are planned and begin to launch [2], [3], such as Starlink and OneWeb, both have tens of thousands of LEO HTS distributed in several

Manuscript received xxx, 2022. This work was supported in part by the National Natural Sciences Foundation of China (NSFC) under Grant 62071141, Grant 61871147, Grant 61831008, and Grant 62027802. in part by the Shenzhen Basic Research Program under Grant GXWD20201230155427003-20200822165138001, in part by the Natural Science Foundation of Guangdong Province under Grant 2020A1515010505, in part by the Guangdong Science and Technology Planning Project under Grant 2018B030322004, and in part by the Major Key Project of PCL under Grant PCL2021A03-1. (*Corresponding author: Jian Jiao.*)

Q. Hu, J. Jiao, S. Wu, and Q. Zhang are with the Communication Engineering Research Centre, Harbin Institute of Technology (Shenzhen), Shenzhen 518055, China, and also with Peng Cheng Laboratory, Shenzhen 518055, China (e-mail: 20S152060@stu.hit.edu.cn; jiaojian@hit.edu.cn; hitwush@hit.edu.cn; zqy@hit.edu.cn).

Y. Wang is with Peng Cheng Laboratory, Shenzhen 518055, China (e-mail: wangy02@pcl.ac.cn).

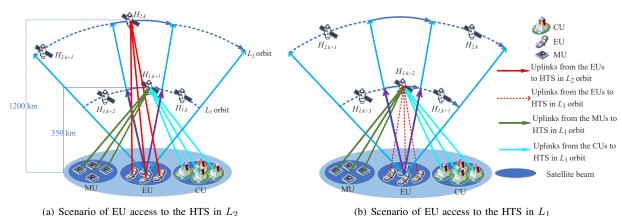
R. Lu is with the Faculty of Computer Science, University of New Brunswick, Fredericton, NB E3B 5A3, Canada, (e-mail: rlu1@unb.ca).

layers at 300  $\sim$  1500 km to provide global coverage, and are expected to support these three types of user equipments (UEs) [4], [5]: 1) Mission critical communications (MCC) UE (CU) requires the packet delay budget of 30 ms with packet error rate (PER) less than  $10^{-6}$  [6]. 2) Massive machine-type communications (mMTC) UE (MU) needs massive connectivity for 4 MUs per km<sup>2</sup> [7]. 3) Enhanced mobile broadband (eMBB) UE (EU) requires stationary connectivity with data rate up to 25 Mbit/s, such as video surveillance and vehicle mounted UE [7]. Moreover, considering the limited line of sight (LoS) duration and capacity of a single LEO HTS to the covered ground UEs, the SpaceX Gen2 system proposes an 8layer LEO HTS constellation at low and very low altitudes [4]. which enables the UEs in the same area to view multiple HTSs. Therefore, we assume a dual-layer LEO HTS constellation in this paper, where the EUs are usually served in the higher layer for longer service duration, and the CUs and MUs are served in the lower layer.

1

On one hand, non-orthogonal multiple access (NOMA) is widely pursued in satellite communications to provide a degree of freedom on power domain by transmitting the superposed signal in the same time-frequency resource block (RB) [8]-[10], which can enhance several key performance indicators (KPI), such as ergodic capacity (EC), outage probability (OP) and system throughput (ST) [11]–[14]: 1) Multiple CUs can simultaneously uplink to HTS via NOMA to reduce the transmission phases [15], since the worst two-way propagation latency is expected to be 26 ms for LEO at 600 km [6]. Note that the PER in the quasi-static fading channel is quickly converged to the OP in finite block-length regime [16], i.e., with  $10^3$  bits packet length, we utilize OP to evaluate the NOMA performance of CUs. 2) Obviously, NOMA is viewed as a potential enabler of mMTC for delay tolerant MUs [17], and the ST can quantitatively depict the successfully accessed MUs. Thus, we can maximize ST under an appropriate OP threshold for the MUs [7], [18]. 3) Further, EUs usually only have the statistical channel state information (CSI) in satellite communications, and the design objective in NOMA scheme for EUs should be maximum EC rather than the actual data rate [8], [11], [14].

On the other hand, there is still lack of work on the multitype services coexistence NOMA scheme for satellite communications. Recently, Ding et al. in [19] have proposed the semigrant free (SGF) NOMA scheme for the grant-based (GB) and grant free (GF) UEs coexistence in terrestrial networks, where several GF UEs can perform power-domain NOMA with one GB UE on the same RB to enhance the system



(a) Scenario of EU access to the HTS in  $L_2$ 

Fig. 1. System model of a dual-layer LEO HTS constellation.

spectral efficiency without deteriorating the OP performance of GB UEs. Moreover, the different channel gains from different received uplink signals lead to a challenge to analyze the uplink NOMA [13], and the imperfect successive interference cancellation (SIC) decoding uplink NOMA schemes for satellite communications are not analyzed yet.

Furthermore, in order to provide broadband access capabilities, HTS adopts the millimeter wave (mmWave) frequency band, such as Ka, V, Q bands [20], [21]. However, the performance of the satellite-to-ground channel in the mmWave band would be seriously affected by rainfall attenuation and the surrounding environment of UEs [22], [23]. To address the characteristics of mmWave band channels, we utilize the widely used log-normal distribution to model our satellite-toground channel [24]–[27], which take two log-normal factors into account for the rainfall attenuation [28]. Moreover, although the EC and OP in log-normal channel are analyzed in OMA systems, there is still lack of derivation for the KPIs in uplink NOMA [23].

Therefore, we propose a multi-type services coexistence handover (MSCH) NOMA scheme in the dual-layer LEO HTS constellation, and the main contributions of this paper are outlined as follows.

- First, we propose the MSCH NOMA scheme to guarantee the KPI requirements of multi-type UEs coexistence in the dual-layer LEO HTS constellation. Inspired by the SGF NOMA, we divide the system bandwidth of lower layer satellites into RBs for CUs and MUs. Specifically, CUs select the RBs as reserved RBs (RRBs) to perform GB NOMA access to satisfy the critical access requirement, and MUs can perform GF NOMA access on the rest RBs as non-reserved RBs (NRBs). Further, the EUs can handover between the two-layer satellites to perform broadband access, thus they can perform NOMA on the higher layer satellites, and joint NOMA access with the CU or MU in the lower layer satellites, respectively.
- Then, considering the different KPI requirements of multi-type UEs and the impact of imperfect SIC, we derive the closed-form expressions of three corresponding KPIs, i.e., OP, ST, and EC in the MSCH NOMA scheme over the log-normal rain attenuation channel. Further,

we propose three uplink NOMA algorithms for each type of UEs when EUs perform access to the higher layer satellite, where the "improve ergodic capacity" (IEC) NOMA algorithm can maximum the EC of EUs under an appropriate OP threshold for each EU, and the "improve outage probability" (IOP) NOMA algorithm can minimize OP of each CU, and the "improve system throughput" (IST) NOMA algorithm can maximum the ST of MUs under an appropriate OP threshold for each MU.

• Moreover, when the EUs handover to the lower layer satellites to coexist with CUs or MUs, we propose two uplink NOMA algorithms for the multi-type UEs coexistence, named "EU and CU coexist" (ECco) and "EU and MU coexist" (EMco) NOMA algorithms, which both can maximize the EC of EUs under an appropriate OP threshold for CUs or MUs, respectively. In addition, we propose a "RB selection" (RBS) algorithm for EUs performing the IEC, ECco or EMco NOMA algorithms on empty RB (eRB), RRB and NRB, respectively, which can jointly achieve the maximum EC of EUs in the lower layer satellites. Finally, simulation results validate the accuracy of our theoretical derivations, and show the superior performance compared with the related "discrete uplink power control" (DUPC) NOMA algorithm [29] and "maximize energy efficiency" (MEE) NOMA algorithm [30].

The rest of the paper is outlined as follows. Section II introduces the dual-layer LEO HTS constellation, the handover transmission scheme, channel model, and the MSCH NOMA scheme. In Section III, we derive the closed-form expressions of the OP, EC and ST, respectively, and then design the NOMA algorithms to meet the different KPI requirements of different types of UEs in Section IV. Section V provides the simulation results united with corresponding analysis. Section VI draws a conclusion.

# II. SYSTEM MODEL AND MSCH NOMA

We assume a dual-layer LEO HTS constellation providing KPI-guaranteed uplink NOMA for the CUs, MUs and EUs as

TABLE I LIST OF ABBREVIATIONS

TABLE II	
PARAMETERS DESCRIPTIONS	

Abbreviation	Full name	Notation	Definition	
LEO	Low-earth orbit		The b-th layer of HTS	
HTS	High-throughput satellite	$t_b$	The LoS duration of the HTS in <i>b</i> -th layer	
5GA	Fifth generation-advance	$\Delta_t$	The time cost for handover of HTS in one layer to	
MSCH	Multi-type service coexistence handover		another	
NOMA	Non-orthogonal multiple access	$x_b$	The time cost for handover of two adjacent HTSs in	
UE	User equipment	0	$L_b$	
MCC	Mission critical communication	$H_{a,b}$	The <i>a</i> -th HTS in the <i>b</i> -th layer	
CU	Mission critical communication user equipment	$S_i^{u,b}$	The <i>i</i> -th frame in the $L_1$ -layer HTS	
mMTC	Massive machine-type communication	$\tilde{S}_{i,j}^{i}$	The <i>j</i> -th subframe of the <i>i</i> -th frame in the HTS	
MU	Massive machine-type communication user equip-	$\overset{\sim i,j}{B}$	The total system bandwidth of HTS	
	ment	$\tilde{D}$	The number of RB in each HTS	
eMBB	Enhanced mobile broadband	$\tilde{N}_c$	The number of CU accessing the RB in $L_1$ layer	
EU	Enhanced mobile broadband user equipment	1.0	HTS	
GF	Grant-free	$N_m$	The number of MU accessing the RB in $L_1$ layer	
SGF	Semi-grant free	- 110	HTS	
GB	Grant-based	$N_e$	The number of EU accessing the RB in $L_1$ layer	
GA	Grant-based access	6	HTS	
KPI	Key performance indicator	P	The maximum transmit power of each UE	
OP	Outage probability	$\alpha_k$	The power control coefficient of UE <sub>k</sub> , where $\alpha_k \in$	
ST	System throughput	c. ĸ	[0,1]	
EC	Ergodic capacity	$\beta_k$	The residual coefficient, where $\beta_k \in [0, 1]$ . Specifi-	
NTN	Non-terrestrial network	$\sim \kappa$	cally, $\beta_k = 0$ means perfect SIC and $\beta_k = 1$ means	
PER	Packet error rate		SIC is failed	
LoS	Line-of-sight	h	The channel gain from UE to HTS	
RB	Resource block	l	The beam gain factor	
RRB	Reserved resource block	$\sigma^2$	The variance of additive white Gaussian noise	
NRB	Non-reserved resource block	$\gamma$	The receiving SINR of UE at HTS	
IEC	Improve ergodic capacity	1		
IOP	Improve outage probability			
IST	Improve system throughput			
ECco	EU and CU coexist	[3] Moreover	we assume that the Doppler shifts caused by	
EMco	EU and MU coexist			
RBS	RB selection	the high dynam	nic LEO HTSs are identical for different UEs in	
eRB	Empty resource block	the same cover	age area due to the high altitude orbit of HTSs	
DUPC	Discrete uplink power control		• •	
MEE	maximize energy efficiency	[31], and set a guard bandwidth as double than the Doppler		
PDF	probability density function	shifts to relieve	e the influence of Doppler shifts on the system	
SINR	Signal-to-interference and noise ratio	[32]. In addition, the MUs and CUs only access the $L_1$ layer		
MUMS	Multi-user multi symbol			
mmWave	Millimeter wave	HTS due to the low propagation latency and their short packet		
SIC	Successive interference cancellation	communication	is [2]. For convenience, the related notations are	
CSI	Channel state information	summarized in	Table II.	
AWGN	Additive white Gaussian noise			
RAP	Random access preamble			
RAM	Resource acquisition message			
CID	CU identifier	A. Handover T	Fransmission Scheme for EUs	
PI	Power information	XX 7' .1 . 1		
RAR	Random access response	Without loss	s of generality, we assume that EUs perform	
RRC	Radio resource control	long-term stati	onary connectivity (e.g., video surveillance,	
SSS	Switching service signal	•	ted and fix installation services [7]). Note that	
RAS	Resource allocation signal			
EID	EU identifier		on of HTS in $L_2$ is longer than that of $L_1$ .	
CDF	Cumulative distribution function	Therefore, the	EUs usually prefer access to the HTS in $L_2$	
RA	Random access		duration to reduce the frequent handovers as	
<u>і\Л</u>	Kandolli access	TOI TOILGET LOS	duration to reduce the frequent handovers as	

shown in Fig. 1 [4], [5]<sup>1</sup>. The area sandwiched by the purple arrows in Fig. 1 is the actual communication range of the UEs for high-quality access, while the area sandwiched by the blue arrows on the leftmost and rightmost sides is the theoretical LoS range of the ground UEs. There are multiple HTSs in  $L_1$ and  $L_2$ , where the LEO HTSs in  $L_1$  layer are with a lower altitude of 350 km, and the LEO HTSs in  $L_2$  layer are about 1200 km [2], and the number of HTSs in  $L_1$  is large enough to form a seamless coverage for the service area, while the UEs in this coverage area only access one HTS in its LoS duration shown in Fig. 2.

in  $L_2$ .

Further, we assume that the LoS of HTSs at  $L_2$  and  $L_1$ 

are  $t_2$  and  $t_1$ , respectively, and the time cost for handover of

two adjacent HTSs in  $L_1$  and  $L_2$  are  $x_1$  and  $x_2$ , respectively.

Moreover, the time cost for handover from an HTS in  $L_2$  to

an HTS in  $L_1$  is  $\Delta_t$ , as well as from an HTS in  $L_1$  to an HTS

access to HTSs in  $L_1$  and  $L_2^2$ , respectively. Therefore, the

handover transmission scheme for EUs has three options due

 ${}^{2}R_{1}$  and  $R_{2}$  are related to the system parameters and the proposed IEC,

ECco and EMco NOMA algorithms with RBS algorithm at  $L_1$ , and the

to the system parameters as shown in Fig. 2.

proposed IEC NOMA algorithm at  $L_2$ , respectively.

In addition, let  $R_1$  and  $R_2$  denote the EC of EUs to perform

<sup>&</sup>lt;sup>1</sup>Different types of UEs are grouped as shown in Fig. 1, however, these UEs are coexisting in the same area in practical.

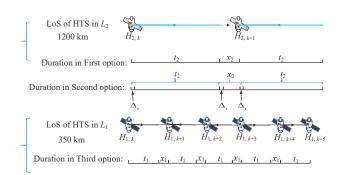


Fig. 2. Schematic diagram of EUs perform handovers between HTSs in  $L_1$ and  $L_2$ .

The first option is the EUs only perform handover to the adjacent HTSs in  $L_2$  if  $x_2 \leq 2\Delta_t$ , and the long-term EC, which is the average EC of the UEs during a period of uplink transmission, which can be expressed as

$$E_1 = \frac{t_2 R_2}{t_2 + x_2}.$$
 (1)

If  $x_2 > 2\Delta_t$ , the second option is the EUs can handover to an HTS at  $L_1$  with  $\Delta_t$  when the LoS of current HTS  $H_{2,k}$ at  $L_2$  is finished, and the EUs would handover back to the  $H_{2,k+1}$  after  $x_2$  at  $L_1$ . Thus, the long-term EC of EUs can be expressed as

$$\frac{(t_2 - \Delta_t)R_2 + (x_2 - \Delta_t - nx_1)R_1}{t_2 + x_2} \le E_2$$

$$\le \frac{(t_2 - \Delta_t)R_2 + (x_2 - \Delta_t)R_1}{t_2 + x_2}.$$
(2)

where n is the largest number of HTSs at  $L_1$  that the EUs need to perform handover within  $x_2$ .

The third option is the EUs only utilize the HTSs at  $L_1$  for uplink transmission, which may experience frequent handovers during the transmission due to the short LoS duration of HTS in  $L_1$ , and the long-term EC can be expressed as

$$E_3 = \frac{t_1 R_1}{t_1 + x_1}.$$
 (3)

Therefore, the EUs can select an appropriate option to perform handover according to the above long-term EC performance, which is determined by the relationship of  $x_2$  and  $2\Delta_t$  in the dual-layer LEO HTS constellation.

# B. Channel Model

We utilize the widely used log-normal distribution to model the mmWave channel in our dual-layer LEO HTS constellation [23]. The probability density function (PDF) of the channel gain  $|h_{k,a,b}|^2$  from the k-th terrestrial UE  $U_k$  to the a-th HTS in the *b*-th layer  $H_{a,b}$  is given by

$$f_{|h_{k,a,b}|^2}(x) = \frac{\varepsilon_{k,a,b}^{\mathcal{M}_{k,a,b}}}{\Gamma\left(\mathcal{M}_{k,a,b}\right)} x^{\mathcal{M}_{k,a,b}-1} \exp\left(-\varepsilon_{k,a,b} \cdot x\right), \quad (4)$$

where  $\Gamma(\cdot)$  is the Gamma function,  $\varepsilon_{k,a,b} = \mathcal{M}_{k,a,b}/\Omega_{k,a,b}$ , and  $\mathcal{M}_{k,a,b} = 1/(\exp(\sigma_{k,a,b}) - 1)$  is a measure of the fading severity, and  $\Omega_{k,a,b} = q_{k,a,b}\sqrt{\frac{\mathcal{M}_{k,a,b}+1}{\mathcal{M}_{k,a,b}}}$  represents the average power of each link, where  $q_{k,a,b} = \exp(\mu_{k,a,b})$  is the constant area average power, and  $\mu_{k,a,b}$  and  $\sigma_{k,a,b}$  represent the lognormal location and scale parameters, respectively. Without loss of generality, assume that the HTSs in the same layer have the same SIC performance, then we can ignore the subscript a in the following.

# C. Signal Model

Assume that the *i*-th RB can accommodate at most  $Z_i$  UEs by employing NOMA [19], and each UE can only access one RB. Without loss of generality, the signals of  $Z_i$  UEs in the *i*-th RB are arranged in a descending order according to their channel gain  $h_{k,b}$  and gain factor  $l_{k,b}$  between  $U_k$  and  $H_b$  as follows

$$h_{1,b}l_{1,b}| \ge \dots \ge |h_{Z_i,b}l_{Z_i,b}|,$$
 (5)

where  $l_{k,b} = \sqrt{G_b \cdot G_k / F_{k,b}}$ , and  $G_b$  and  $G_k$  are the antenna gain at  $H_b$  and  $U_k$ , respectively, and  $F_{k,b} = 92.4 + 20 \log f + 10 \log f$  $20 \log d_{k,b}$  is the free space path loss between  $U_k$  and  $H_b$ , which includes the distance  $d_{k,b}$  between  $U_k$  and  $H_b$ , and the carrier frequency f of  $U_k$ .

Then,  $H_b$  utilize SIC to recover the received signal at each RB. Considering the impact of imperfect SIC, the signalto-interference and noise ratio (SINR) of  $U_k$  in  $H_b$  can be expressed as:

$$\gamma_{k,b} = \frac{\alpha_{k,b} P_{k,b} |h_{k,b} l_{k,b}|^2}{X + Y + \sigma^2},$$
(6)

where

1)  $X = \sum_{j=k+1}^{Z} P_{j,b} \alpha_{j,b} |h_{j,b} l_{j,b}|^2$ : Indicates the interference caused by other UEs in the same NOMA group with worse signals than that of  $U_k$ , where  $P_{j,b}$  is the transmit power of  $U_j$ , and  $0 \le \alpha_{k,b} \le 1$  is the power coefficient of  $U_k$  which can be adjusted by  $G_b$  and  $G_k$ .

2)  $Y = \sum_{i=1}^{k-1} P_{i,b} \beta_{i,b} \alpha_{i,b} |h_{i,b} l_{i,b}|^2$ : Represents the residual component of  $U_k$ 's signal after SIC, where  $\beta_{i,b}$  represents the residual coefficient after the *i*-th SIC at  $H_b$ .

3)  $\sigma^2$ : Additive white Gaussian noise (AWGN) with zero mean and variance  $\sigma^2$ .

#### D. MSCH NOMA Scheme

In our MSCH NOMA scheme in the dual-layer LEO HTS constellation, each HTS has multiple RBs to provide SGF NOMA transmission. First, considering the HTSs in  $L_1$  as shown in Fig. 3, recall that the RBs selected by CUs are RRBs, the rest RBs selected by MUs called NRBs, and the RBs not selected by any CU and MU are eRBs. Moreover, the LoS duration  $t_1$  in each HTS  $H_1$  is divided into K frames, where the CUs and MUs are randomly activated and perform SGF NOMA at the beginning of each frame. Further, each frame  $S_i$ can be further divided into three subframes as  $S_{i,1}$ ,  $S_{i,2}$  and  $S_{i,3}$ , where  $S_{i,1}$  and  $S_{i,1} + S_{i,2}$  are the packet delay budgets of CUs and MUs, respectively.

Therefore, as shown in Fig. 3 (a), there are only CUs and MUs accessing to the HTS in  $L_1$  when the EUs access to the HTS in  $L_2$ . The CUs perform GB NOMA in the RRBs,

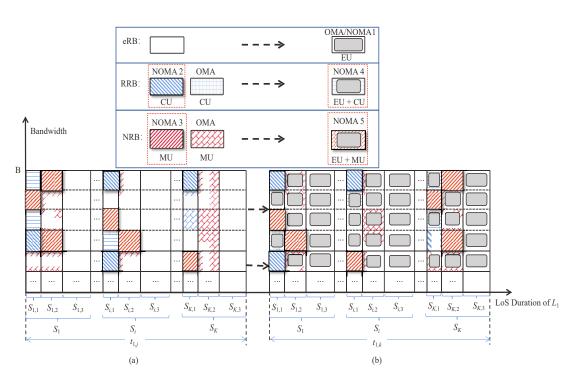


Fig. 3. The illustration of RBs and frames in our MSCH NOMA scheme. (a) CUs and MUs access to the HTS in  $L_1$ , (b) EUs access to the HTS in  $L_1$  and perform coexist NOMA with CUs and MUs.

and the MUs perform GF NOMA the NRB. When the EUs perform handover to the HTS in  $L_1$ , the CUs, MUs and EUs perform SGF NOMA to the HTS in  $L_1$  as shown in Fig. 3 (b). Specifically, the proposed MSCH NOMA scheme is designed under the following assumptions: 1) The CSI remains constant during  $S_i$  and randomly varies between different  $S_i$ . 2) Each RB corresponds to a random access preamble (RAP), and HTS can distinguish the selected RBs by the RAPs from received signals [35], [36]. 3) HTS can identify the number of uplink UEs and acquire the CSI of each UE in each RB through the new transceiver structure proposed in [37], which consists of a secondary preamble and a multi-user multi symbol (MUMS) detector. 4) The CUs would finish their service in  $S_{i,1}$ , and the MUs can perform random access with RRB in  $S_{i,2}$ , and with NRB in  $S_{i,1}$  and  $S_{i,2}$  as shown in Fig. 3.

Furthermore, the proposed MSCH NOMA scheme has three parts: 1) The SGF random access protocols for CUs, MUs and EUs as shown in Fig. 4; 2) The resource acquisition messages (RAM) generator as shown in Fig. 5; 3) The NOMA algorithms for different UEs, which are designed in Section IV. In the following, we introduce the first and second parts of the MSCH NOMA scheme.

# E. SGF Random Access Protocols in MSCH NOMA Scheme

# 1) GB Random Access Protocol for CUs:

**Step 1** The HTS broadcasts all RAPs at the beginning of  $S_{i,1}$  as shown in Fig. 4 (a).

**Step 2** The CUs upload the selected RAPs and their CU identities (CIDs) to mark the RRBs, and transmit power information (PI).

Step 3 The HTS broadcasts random access response (RAR),

including CSI, maximum data rate and synchronization message, and RAM1 to all UEs.

**Step 4** The CUs that get the successful RAR from the HTS make a radio resource control (RRC) connection request by sending their CIDs to the HTS.

Step 5 The HTS sends ACKs to all granted access CUs.

**Step 6** The granted access CUs select appropriate NOMA algorithm according to the RAR and RAM1, and begin to upload data.

2) GF Random Access Protocol for MUs:

**Step 1** The HTS broadcasts all RAPs at the beginning of  $S_{i,1}$  as shown in Fig. 4 (b).

**Step 2** The MUs upload the selected RAPs to mark the NRBs and transmit PI.

**Step 3** The HTS broadcasts RAR and RAM2 to all terrestrial UEs.

**Step 4** The MUs (part 1) select appropriate NOMA algorithm according to the RAR and RAM2, and begin to uplink data as shown in Fig. 3, and the rest of MUs that selecting RRBs (part 2) are waiting in the  $S_{i,1}$ .

**Step 5** At the beginning of  $S_{i,2}$ , the part2 MUs upload the re-selected RAPs to mark NRBs and transmit PI.

**Step 6** The HTS broadcasts RAR and RAM3 to the part 2 MUs.

**Step 7** The part 2 MUs select appropriate NOMA algorithm according to the RAR and RAM3, and begin to upload data. *3) GB Access Protocol for EUs*:

**Step 0** The EUs perform GB NOMA access to the HTS in  $L_2$  for the longer LoS duration [35] as shown in Fig. 4 (c). When the condition of the first option in the handover transmission scheme is satisfied, the EUs wait the time cost  $x_2$  after  $t_2$  to perform handover to the next HTS in  $L_2$ . Otherwise,

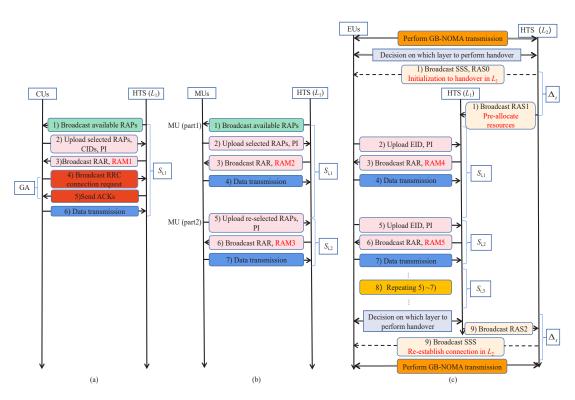


Fig. 4. The SGF random access protocols for CUs, MUs and EUs. (a) GB random access protocol for CUs. (b) GF random access protocol for MUs. (c) GB access protocol for EUs.

the current served HTS in  $L_2$  informs an appropriate HTS in  $L_1$  that the EUs would perform handover with time cost  $\Delta_t$  [2], and the GB access protocol for EUs in  $L_1$  is as follows.

**Step 1** The current served HTS in  $L_2$  broadcasts switching service signals (SSS) and resource allocation signal 0 (RAS0) to EUs, and transmits the EU identities (EIDs) in RAS1 to the HTS in  $L_1$ .

**Step 2** After receiving SSS, the EUs begin to upload PI to the  $L_1$  layer HTS.

**Step 3** The  $L_1$  layer HTS broadcasts the RAR and RAM4 to the EUs.

**Step 4** The granted access EUs selects the appropriate RBs and corresponding NOMA algorithm according to RAR and RAM4 for data transmission.

**Step 5** At the beginning of the  $S_{i,2}$ , the EUs upload EIDs and PI to the  $L_1$  layer HTS.

**Step 6** The  $L_1$  layer HTSs broadcasts the RAR and RAM5 to the EUs.

**Step 7** The granted access EUs selects the appropriate RBs and corresponding NOMA algorithm according to RAR and RAM5 for data transmission.

**Step 8** Repeat above **Steps 5-7** in  $S_{i,3}$ .

**Step 9** Repeat above **Steps 2-8** until the EUs can perform handover to the  $L_2$  layer HTS. Then, the  $L_1$  layer HTS transmits RAS2 to the  $L_1$  layer HTS with the time cost  $\Delta_t$ , and then the  $L_2$  layer HTS broadcasts the SSS to the EUs.

**Step 10** Then, EUs begin to perform GB NOMA access to the  $L_2$  layer HTS.

## F. RAM Generator in MSCH NOMA Scheme

The generation logic of RAM signals in above SGF random access protocols is shown in Fig. 5. When the  $L_1$  layer HTS receives RAPs, CIDs, EIDs and PI from CUs, MUs and EUs, as well as RAS from  $L_2$  layer HTS, it estimates the CSI of UEs according to the PIs and identifies the number of CUs and MUs in different RBs. In addition, the HTS utilizes the RBS algorithm in Section IV-F to select an appropriate RB for EUs. Therefore, the number of CUs, MUs and EUs in each RB can be obtained as  $N_c$ ,  $N_m$  and  $N_e$ , respectively. Then, the HTS generates access denied signal as (8) in RAM according to  $N_c$ ,  $N_m$ ,  $N_e$  and CSI, or further generates control signals in RAM for the UEs to select appropriate NOMA algorithms.

6

# III. DERIVATION OF KPIS

In this section, we first derive specific KPIs (i.e., OP, EC and ST) to measure the performance of different types of UEs.

#### A. Problem Formulation Under Two UEs Model

Note that the number of UEs in power domain NOMA is usually small in practical [11], thus, we set Z = 2 in each RB to derive the closed-form expressions of KPIs in the following. First, recall Eq. (6), the SINR of  $U_1$  at  $H_b$  can be expressed as:

$$\gamma_{1,b} = \frac{\alpha_{1,b} P_{1,b} |h_{1,b}|^2 |l_{1,b}|^2}{\alpha_{2,b} P_{2,b} |h_{2,b}|^2 |l_{2,b}|^2 + \sigma^2},\tag{7}$$

and the SINR of  $U_2$  at  $H_b$  is

$$\gamma_{2,b} = \frac{\alpha_{2,b} P_{2,b} |h_{2,b}|^2 |l_{2,b}|^2}{\beta_{1,b} \cdot \alpha_{1,b} P_{1,b} |h_{1,b}|^2 |l_{1,b}|^2 + \sigma^2}.$$
(8)

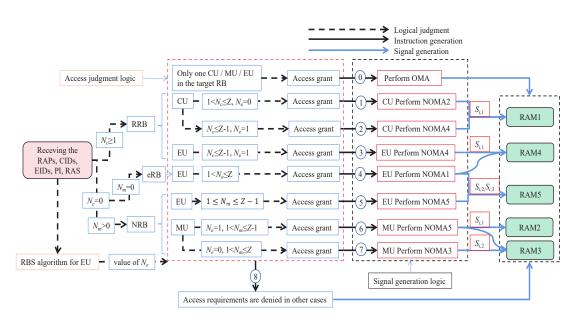


Fig. 5. Logic generation diagram of RAM signal in RRB and NRB for CU, MU and EU.

# B. EC Performance Analysis

Recall that EC is defined as the expected value of instantaneous mutual information of SINR  $\gamma_{k,b}$  of  $U_k$  at  $H_b$ , and we have

$$C(\gamma_{k,b}) = E[\log(1+\gamma_{k,b})]. \tag{9}$$

With the help of [39, Eq. (6)],  $C(\gamma_{k,b})$  can be well approximated as

$$C(\gamma_{k,b}) = \log_2(e) \cdot \left\{ \ln[1 + E(\gamma_{k,b})] - \frac{E(\gamma_{k,b}^2) - E(\gamma_{k,b})^2}{2(1 + E(\gamma_{k,b}))^2} \right\}$$
(10)

Further, with the help of [38, Eq. (6.455.1)], we can get the closed-form expression of  $E(\gamma_{1,b})$  and  $E(\gamma_{1,b}^2)$  for  $U_1$  at  $H_b$  as follows

$$E(\gamma_{1,b}) = \frac{\rho_{1,b}\alpha_{1,b}\Gamma\left(\mathcal{M}_{1,b}+1\right)}{\left(1 + \rho_{2,b}\alpha_{2,b}\frac{\Gamma\left(\mathcal{M}_{2,b}+1\right)}{\varepsilon_{2,b}\Gamma\left(\mathcal{M}_{2,b}\right)}\right)\varepsilon_{1,b}\Gamma\left(\mathcal{M}_{1,b}\right)}, \quad (11)$$

and

$$E(\gamma_{1,b}^{2}) = \frac{\rho_{1,b}^{2}\alpha_{1,b}^{2}\Gamma\left(\mathcal{M}_{1,b}+2\right)}{\left(1+\rho_{2,b}\alpha_{2,b}\frac{\Gamma(\mathcal{M}_{2,b}+1)}{\varepsilon_{2,b}\Gamma(\mathcal{M}_{2,b})}\right)^{2}\varepsilon_{1,b}^{2}\cdot\Gamma\left(\mathcal{M}_{1,b}\right)}, \quad (12)$$

where  $\rho_{i,b} = \frac{P_{i,b}}{\sigma^2} |l_{i,b}|^2$  denotes the transmission average signal-noise ration (SNR) of  $U_i$  at  $H_b$ . Then, we can get EC  $C(\gamma_{1,b})$  for  $U_1$  at  $H_b$  by substituting Eq. (11) and Eq. (12) into Eq. (10).

Similarly, we can obtain the closed-form expression of  $E(\gamma_{2,b})$  and  $E(\gamma_{2,b}^2)$  for  $U_2$  at  $H_b$  as follows

$$E(\gamma_{2,b}) = \frac{\rho_{2,b}\alpha_{2,b}\Gamma\left(\mathcal{M}_{2,b}+1\right)}{\left(1+\beta_{1,b}\rho_{1,b}\alpha_{1,b}\frac{\Gamma\left(\mathcal{M}_{1,b}+1\right)}{\varepsilon_{1,b}\Gamma\left(\mathcal{M}_{1,b}\right)}\right)\varepsilon_{1,b}\Gamma\left(\mathcal{M}_{1,b}\right)},$$
(13)

and

$$E(\gamma_{2,b}^{2}) = \frac{\rho_{2,b}^{2} \alpha_{2,b}^{2} \Gamma\left(\mathcal{M}_{2,b} + 2\right)}{\left(1 + \beta_{1,b} \rho_{1,b} \alpha_{1,b} \frac{\Gamma(\mathcal{M}_{1,b}+1)}{\varepsilon_{1,b} \Gamma(\mathcal{M}_{1,b})}\right)^{2} \varepsilon_{1,b}^{2} \cdot \Gamma\left(\mathcal{M}_{1,b}\right)},$$
(14)

and we can obtain EC  $C(\gamma_{2,b})$  for  $U_2$  at  $H_b$  by substituting Eq. (13) and Eq. (14) into Eq. (10). The detailed derivations for Eqs. (11)-(14) are shown in the Appendix A.

# C. OP Performance Analysis

The OP of each UE is defined as the probability that the instantaneous SINR  $\gamma_{k,b}$  of  $U_k$  at  $H_b$  lower than a given SINR threshold  $\gamma_{k,b}^{\text{th}}$ , and we have

$$F_{k,b}(\gamma_{k,b}^{\mathrm{th}}) = \Pr(\gamma_{k,b} < \gamma_{k,b}^{\mathrm{th}}), \qquad (15)$$

where  $F_{k,b}(\gamma_{k,b}^{\text{th}})$  is the cumulative distribution function (CDF) of  $\gamma_{k,b}$ .

With the help of [38, Eq. (3.351.2)], we can obtain the closed-form expression of OP for  $U_1$  at  $H_b$  as follows

$$F_{1,b}\left(\gamma_{1,b}^{\mathrm{th}}\right) = 1 - \frac{\Gamma\left(\mathcal{M}_{1,b}, \frac{\varepsilon_{1,b}\gamma_{1,b}^{\mathrm{th}}(1+\rho_{2,b}\alpha_{2,b}\frac{\Gamma(\mathcal{M}_{2,b}+1)}{\varepsilon_{2,b}\Gamma(\mathcal{M}_{2,b})}\right)}{\rho_{1,b}\alpha_{1,b}}\right)}{\Gamma\left(\mathcal{M}_{1,b}\right)}.$$
(16)

Similarly, we can obtain the closed-form expression of OP for  $U_2$  at  $H_b$  via [38, Eq. (3.351.2)] as follows

$$F_{2,b}\left(\gamma_{2,b}^{\mathrm{th}}\right) = 1 - \frac{\Gamma\left(\mathcal{M}_{2,b}, \frac{\varepsilon_{2,b}\gamma_{2,b}^{\mathrm{th}}(1+\beta_{1,b}\rho_{1,b}\alpha_{1,b}\frac{\Gamma(m_{1,b}+1)}{\varepsilon_{1,b}\Gamma(\mathcal{M}_{1,b})})}{\rho_{2,b}\alpha_{2,b}}\right)}{\Gamma\left(\mathcal{M}_{2,b}\right)}$$
(17)

The detailed derivations for Eq. (16) and Eq. (17) are shown in the Appendix B.

Further, note that the channel conditions of  $U_1$  and  $U_2$  are independent, then the joint OP expression of this NOMA group

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8

at  $H_b$  can be obtained as

$$F_{b}\left(\gamma_{b}^{\mathrm{th}}\right) = 1 - \Pr\left(\gamma_{1,b} > \gamma_{1,b}^{\mathrm{th}}\right) \Pr\left(\gamma_{2,b} > \gamma_{2,b}^{\mathrm{th}}\right)$$
$$= 1 - \frac{\Gamma\left(\mathcal{M}_{1,b}, \frac{\varepsilon_{1,b}\gamma_{1,b}^{\mathrm{th}}(1+\rho_{2,b}\alpha_{2,b}\frac{\Gamma(\mathcal{M}_{2,b}+1)}{\varepsilon_{2,b}\Gamma(\mathcal{M}_{2,b})}\right)}{\Gamma(\mathcal{M}_{1,b})}\right)}{\Gamma(\mathcal{M}_{1,b})}$$
$$\cdot \frac{\Gamma\left(\mathcal{M}_{2,b}, \frac{\varepsilon_{2,b}\gamma_{2,b}^{\mathrm{th}}(1+\beta_{1,b}\rho_{1,b}\alpha_{1,b}\frac{\Gamma(\mathcal{M}_{1,b}+1)}{\varepsilon_{2,b}\Gamma(\mathcal{M}_{1,b})}\right)}{\Gamma(\mathcal{M}_{2,b})}}{\Gamma(\mathcal{M}_{2,b})}.$$
(18)

With the given SINR threshold  $\gamma_{i,b}^{\text{th}}$ , we can establish two inequations according to Eq. (7) and Eq. (8) as follows, which should be satisfied by  $\alpha_i$  when decoding the signal of  $U_1$  at  $H_b$ ,

$$\frac{\alpha_{1,b}\rho_{1,b}|h_{1,b}|^2}{\alpha_{2,b}\rho_{2,b}|h_{2,b}|^2 + 1} \ge \gamma_{1,b}^{\text{th}},\tag{19}$$

and

$$\frac{\alpha_{2,b}\rho_{2,b}|h_{2,b}|^2}{\beta_{1,b} \cdot \alpha_{1,b}\rho_{1,b}|h_{1,b}|^2 + 1} \ge \gamma_{2,b}^{\text{th}}.$$
 (20) 10

## D. ST Performance Analysis

The ST of  $U_k$  at  $H_b$  can be expressed as the product of EC and decoding success probability  $Pr_{(k,b)}$  of each UE, which can be expressed as

$$T_{k,b} = C(\gamma_{k,b}) \Pr_{(k)}(\gamma_{k,b}^{\mathrm{th}}), \qquad (21)$$

where  $\Pr_{(k,b)}(\gamma_{k,b}^{\text{th}}) = 1 - F_{k,b}(\gamma_{k,b}^{\text{th}}).$ 

# IV. ALGORITHMS DESIGN FOR MSCH NOMA SCHEME

In this section, we focus on the design of NOMA algorithms to guarantee the KPI requirements of different types of UEs in our MSCH NOMA scheme, and we propose the RBS algorithm to enhance the EC of EUs in  $L_1$  layer HTS.

#### A. IEC Algorithm for EU

As shown in Fig. 4 (c) in the aforementioned Section II-E, when EUs perform NOMA to the HTS in  $L_2$  and the eRBs of the HTS in  $L_1$ , considering the high data rate requirements of EUs, the optimization goal is maximizing the sum EC  $C_{sum}$ of each EU NOMA group, and the optimization problem is established as follows

$$\max C_{sum} = C(\gamma_{e_1,b}) + C(\gamma_{e_2,b}), \qquad (22a)$$

$$s.t.: 0 \le \alpha_{e_k,b} \le 1, \tag{22b}$$

$$F_{e_k,b}(\gamma_{e_k,b}^{\text{th}}) \le \xi_{e_i,b}, \qquad (22c)$$

where (22b) indicates the power coefficient  $\alpha_{e_k,b}$  for  $EU_k$  at  $H_b$ , (22c) guarantees an OP threshold  $\xi_{e_i,b}$  for each EU at  $H_b$ .

Recall that  $EU_1$  has better channel condition, and  $C(\gamma_{e_1,b})$  has higher impact on  $C_{sum}$  than  $C(\gamma_{e_2,b})$ . Then, we can straightforwardly derive that  $\alpha_{e_1,b}$  is strictly positive with  $C(\gamma_{e_1,b})$  and  $\alpha_{e_2,b}$  is negative with  $C(\gamma_{e_1,b})$ , which is proofed in Appendix C. Therefore, we can maximize  $C_{sum}$  with  $\alpha_{e_1,b} = 1$ . In addition, according to Eq. (16) and Eq. (17),

# **Algorithm 1:** IEC Algorithm for EUs and IST Algorithm for MUs

**Input:**  $\mathcal{M}_{k,b}$ ,  $\varepsilon_{k,b}$ ,  $\beta_{k,b}$ ,  $\gamma_{k,b}^{\text{th}}$ ,  $\rho_{k,b}$ ,  $h_{k,b}$ ,  $l_{k,b}$ ,  $\xi_{k,b}$ , current system transmit power  $P_{cur}$ , maximum UE power  $P_{max}$ , step length  $\Delta_{\alpha_m} > 1$ , iterations  $\chi$ ,  $N_c$ ;

**Output**: Power coefficients  $\alpha_{1,b}$  and  $\alpha_{2,b}$ ;

1 if 
$$N_c = 1$$
 or  $N_e = 1$  then

**2 Return**  $\alpha_{1,b} = 1$ , and  $\alpha_{2,b} = 0$ ;

# 3 end

7 8 9

12 13

14

15

16 17 18

19 20 21

22

23

- 4 for  $P_{cur} \leq P_{max}$  do 5 | Initialize right =
- Initialize right = 1 and left = 0;
- 6 Substitute  $\alpha_{1,b} = 1$  and  $\alpha_{2,b} = left$  into Eq. (17) to get  $F_{2,b}(\gamma_{2,b}^{\text{th}})$ .

for 
$$\chi > 0$$
 do  

$$\begin{vmatrix}
\text{for } \chi > 0 \text{ do} \\
\text{let } mid = left + \frac{left + right}{\Delta_{\alpha_m}}, \\
\text{Substitute } \alpha_{1,b} = 1 \text{ and } \alpha_{2,b} = mid \text{ into Eq. (17)} \\
\text{to update } F_{2,b}(\gamma_{2,b}^{\text{th}}). \\
\text{if } F_{2,b}(\gamma_{2,b}^{\text{th}}) > \xi_{2,b} \text{ then} \\
\mid left = mid; \\
\text{else} \\
\begin{vmatrix}
\text{Substitute } \alpha_{1,b} = 1 \text{ and } \alpha_{2,b} = mid \text{ into Eq.} \\
(16) \text{ to update } F_{1,b}(\gamma_{1,b}^{\text{th}}). \\
\text{if } F_{1,b}(\gamma_{2,b}^{\text{th}}) > \xi_{1,b} \text{ then} \\
\mid right = mid; \\
\text{else} \\
\mid break; \\
\text{end} \\
\text{end} \\
\chi = \chi - 1; \\
\text{end} \\
\text{Return } \alpha_{1,b} \text{ and } \alpha_{2,b};
\end{aligned}$$

we can derive that  $\alpha_{e_2,b}$  is strictly positive with  $F_{e_1,b}(\gamma_{e_1,b}^{\text{th}})$ , and negative with  $F_{e_2,b}(\gamma_{e_2,b}^{\text{th}})$ . Thus, in order to satisfy the OP threshold  $\xi_{e_i,b}$  in (22c), we should find a minimum  $\alpha_{e_2,b}$ to satisfy  $F_{e_k,b}(\gamma_{e_k,b}^{\text{th}}) \leq \xi_{e_k,b}$  according to Eq. (19) and Eq. (20). Therefore, we propose the IEC algorithm as NOMA 1 in Fig. 3, which is concluded in Algorithm 1.

#### B. IOP Algorithm for CU

First, since CUs and MUs only access the  $L_1$  layer HTS, we can ignore the subscript b in the following.

Then, according to Eq. (44) in Appendix A, the OP of  $U_1$  at  $H_b$  can be expressed as  $F_1(\gamma_1^{\text{th}}) = 1 - \int_{\frac{\gamma_1^{\text{th}}(\alpha_2\rho_{2,b}|h_{2,b}|^2+1)}{\alpha_{1,b}\rho_1}} f_{|h_1|^2}(y) dy$ , and  $f_{|h_1|^2}(y)$  is larger than zero. Therefore,  $\int_{\frac{\gamma_1^{\text{th}}(\alpha_2\rho_2|h_2|^2+1)}{\alpha_{1}\rho_1}}^{\infty} f_{|h_1|^2}(y) dy$  is positive with  $\alpha_1$ , which means  $F_1(\gamma_1^{\text{th}})$  has negative relationship with  $\alpha_1$ . Similarly, we can derive that each  $\alpha_k$  has a negative relationship with  $F_k(\gamma_k^{\text{th}})$ .

Therefore, when CUs perform NOMA on RRBs of the HTS in  $L_1$  as shown in Fig. 4 (a) in the aforementioned Section II-E, considering the high reliability requirements of CUs, the

9

optimization problem is to minimize the OP  $F_k(\gamma_k^{\text{th}})$  of both CUs, which indicates the power constraints of  $\alpha_{c_k} = 1$  due to the negative relationship for each  $\alpha_{c_k}$  with  $F_k(\gamma_k^{\text{th}})$ , and we have

$$\min\max F_k(\gamma_k^{\rm th}),\tag{23a}$$

$$s.t.: \log\left(1 + \gamma_{c_k}^{\text{th}}\right) \ge R_{c_k}, \tag{23b}$$

where (23b) is the SINR threshold  $\gamma_{c_k}^{\text{th}}$  to guarantee the required data rate  $R_{c_k}$  of the k-th CU.

Moreover,  $\gamma_{c_k}^{\text{th}}$  in (23c) can be expressed as

$$\gamma_{c_k}^{\text{th}} \ge 2^{R_{c_k}} - 1.$$
 (24)

Note that a fixed SINR threshold  $\gamma_{c_k}^{\text{th}}$  would lead to error floor [40]. Therefore, we set a varying SINR threshold  $\gamma_{c_k}^{\text{th}}$  as follows.

Since (23a) is established for both CUs in the NOMA group, it can be expressed as

$$F_{c_1}(\gamma_{c_1}^{\text{th}}) = F_{c_2}(\gamma_{c_2}^{\text{th}}).$$
 (25)

By substituting Eq. (16), Eq. (17) into Eq. (25), we can get the expression of  $\gamma_{c_k}^{\text{th}}$  to satisfy Eq. (25) as

$$\frac{\gamma_{c_1}^{\text{th}}}{\rho_{c_1}\left(1+\beta_{c_1}\rho_{c_1}\frac{\Gamma(\mathcal{M}_{c_1}+1)}{\varepsilon_{c_1}\Gamma(\mathcal{M}_{c_1})}\right)} = \frac{\gamma_{c_2}^{\text{th}}}{\rho_{c_2}(1+\rho_{c_2}\frac{\Gamma(\mathcal{M}_{c_2}+1)}{\varepsilon_{c_2}\Gamma(\mathcal{M}_{c_2})})}.$$
(26)

Therefore, we can set the varying SINR threshold  $\gamma_{c_k}^{\text{th}}$  as follows:

$$\gamma_{c_{1}}^{\text{th}} = \max\left\{2^{R_{c_{1}}} - 1, \frac{1}{\rho_{c_{1}}\left[1 + \beta_{c_{1}}\rho_{c_{1}}\frac{\Gamma(\mathcal{M}_{c_{1}}+1)}{\varepsilon_{c_{1}}\Gamma(\mathcal{M}_{c_{1}})}\right]}\right\},\tag{27}$$

and

$$\gamma_{c_2}^{\text{th}} = \max\left\{2^{R_{c_2}} - 1, \frac{1}{\rho_{c_2}(1 + \rho_{c_2}\frac{\Gamma(\mathcal{M}_{c_2} + 1)}{\varepsilon_{c_2}\Gamma(\mathcal{M}_{c_2})})}\right\}.$$
 (28)

Therefore, we can solve (23a) by calculating Eq. (27) and Eq. (28), which is the NOMA 2 in Fig. 3.

## C. IST Algorithm for MU

Further, as shown in Fig. 4 (b) in the aforementioned Section II-E, when MUs perform NOMA on the NRBs of the HTS in  $L_1$ , considering the massive connectivity requirements of MUs, the optimization problem is maximizing the sum ST  $T_{sum}$  of each MU NOMA group as follows,

$$\max T_{sum} = T_{m_1} + T_{m_2}, \tag{29a}$$

$$s.t.: 0 \le \alpha_{m_k} \le 1, \tag{29b}$$

$$F_{m_k}(\gamma_{m_k}^{\text{th}}) \le \xi_{m_k},\tag{29c}$$

where (29b) is the power coefficient  $\alpha_{m_k}$ , (29c) guarantees the OP performance of each MU at H.

Note that  $\Pr_{(m_k)}(R_{m_k}^{\text{th}})$  is close to 1 under the condition of high SNR, thus,  $T_{m_k}$  approaches to  $C(\gamma_{m_k})$ . Therefore, the optimization problem (29a) is similar to (22a), and the IST algorithm is similar to the IEC Algorithm as shown in Algorithm 1, which is the NOMA 3 in Fig. 3.

#### D. ECco NOMA Algorithm for EU with CU

Moreover, as shown in Fig. 3 (b) and Fig. 4 (c) in the aforementioned Section II-D and Section II-E, respectively, when EUs perform NOMA with CUs on the RRBs of the HTS in  $L_1$ . Considering the stringent requirements of CUs, the signals of CUs have higher priority to perform SIC in the RRBs. Therefore, the SINR of CUs and EUs on RRBs can be expressed as

$$\gamma_c = \frac{\alpha_c \rho_c |h_c|^2}{\alpha_e \rho_e |h_e|^2 + 1},\tag{30}$$

and

$$\gamma_e = \frac{\alpha_e \rho_e |h_e|^2}{\alpha_c \beta_c \rho_c |h_c|^2 + 1}.$$
(31)

In addition, the EC of CU  $C(\gamma_c)$  and EU  $C(\gamma_e)$  should satisfy the inequalities as follows

$$\begin{cases} C(\gamma_e) \ge C_c^{\text{th}}, \\ C(\gamma_c) \ge C_e^{\text{th}}, \end{cases}$$
(32)

where  $C_c^{\text{th}}$  and  $C_e^{\text{th}}$  are the EC requirements of CUs and EUs, respectively. Moreover,  $C_c^{\text{th}}$  is effected by the delay budget of CU [6], and  $C_e^{\text{th}}$  is determined by the data requirement (25 Mbit/s [7]) of EU.

By substituting (10) into (32), we can derive that

$$\begin{cases} \alpha_e \geq \frac{x \cdot \varepsilon_e \Gamma(\mathcal{M}_e)(1+y \cdot \beta_c)}{\rho_e \Gamma(\mathcal{M}_e+1)(1-\beta_c \cdot x \cdot y)} = \partial_e^1, \\ \alpha_c \geq \frac{y \cdot \varepsilon_c \Gamma(\mathcal{M}_c)(1+x)}{\rho_c \Gamma(\mathcal{M}_c+1)(1-\beta_c x \cdot y)} = \partial_c, \end{cases}$$
(33)

where  $x = \left(2^{C_e^{\text{th}}} - 1\right)$ , and  $y = \left(2^{C_e^{\text{th}}} - 1\right)$ .

Further, since the SIC first recovers the signal of CU, the OP  $F_c(\gamma_c^{\text{th}})$  of CU can be expressed as

$$F_{c}\left(\gamma_{c}^{\mathrm{th}}\right) = 1 - \frac{\Gamma\left(\mathcal{M}_{c}, \frac{\varepsilon_{c}\gamma_{c}^{\mathrm{th}}\left(1+\rho_{e}\alpha_{e}\frac{\Gamma\left(\mathcal{M}_{e}+1\right)}{\varepsilon_{e}\Gamma\left(\mathcal{M}_{e}\right)}\right)}{\rho_{c}\alpha_{c}}\right)}{\Gamma\left(\mathcal{M}_{c}\right)}.$$
(34)

Therefore, the optimization goal is maximizing the EC  $C(\gamma_e)$  of EUs under the an appropriate OP threshold  $\xi_c$  for CUs, and the optimization problem is established as follows

$$\max C(\gamma_e), \tag{35a}$$

$$s.t.: \partial_c \le \alpha_c \le 1, \tag{35b}$$

$$\partial_e^1 \le \alpha_e \le 1,$$
 (35c)

$$F_c(\gamma_c^{\rm th}) \le \xi_c. \tag{35d}$$

where (35b) and (35c) indicate the constraints of  $\alpha_c$  and  $\alpha_e$  to satisfy the EC requirements of CU and EU, respectively, and (35d) guarantees the OP of CU  $\xi_c$ .

Considering the high EC requirements of EUs and the positive relationship for  $C(\gamma_e)$  and  $\alpha_e$ , we first initialize  $\alpha_e = 1$ . Then, considering the stringent OP requirement of CU, we need to maximize EC of EU under the OP threshold of CU, which may need further adjust  $\alpha_e$  and  $\alpha_c$ , simultaneously. Thus, we propose the ECco algorithm as NOMA 4 in Fig. 3, which is summarized in Algorithm 2.

10

Algorithm 2: ECco NOMA Algorithm for CU and EU coexist

**Input**:  $\mathcal{M}_k$ ,  $\varepsilon_k$ ,  $\beta_k$ ,  $\gamma_k^{\text{th}}$ ,  $\rho_k$ ,  $h_k$ ,  $l_k$ ,  $\xi_c$ ,  $C_k^{\text{th}}$ ,  $P_{cur}$ ,  $P_{max}$ , step length  $\Delta_{\alpha_k}$ ; **Output**:  $\alpha_c$  and  $\alpha_e$ ; 1 for  $P_{cur} \leq P_{max}$  do Calculate  $\partial_c$  and  $\partial_e^1$  according to Eq. (33); 2 Initialize  $\alpha_e = 1$ , and  $\alpha_c = \min(1, \partial_c)$ . 3 Substitute  $\alpha_e$  and  $\alpha_c$  into Eq. (34) to get  $F_c(\gamma_c^{\text{th}})$ . 4 5 while  $\alpha_c < 1$  do Substitute  $\alpha_e$  and  $\alpha_c$  into Eq. (34) to update 6  $F_c\left(\gamma_c^{\mathrm{th}}\right).$ if  $F_c(\gamma_c^{\text{th}}) > \xi_c$  then  $| \alpha_c = \min(1, \alpha_c + \Delta_{\alpha_c});$ 7 8 else 9 break; 10 end 11 end 12 while  $\alpha_e > \partial_e^1$  do 13 Substitute  $\alpha_e$  and  $\alpha_c$  into Eq. (34) to update 14  $\begin{array}{l} F_{c}\left(\gamma_{c}^{\mathrm{th}}\right),\\ \text{if }F_{c}\left(\gamma_{c}^{\mathrm{th}}\right) > \xi_{c} \text{ then}\\ \mid \alpha_{e} = \max(\partial_{e}^{1}, \alpha_{e} - \Delta_{\alpha_{e}}); \end{array}$ 15 16 else 17 break; 18 19 end end 20 21 end 22 Return  $\alpha_c$  and  $\alpha_e$ ;

# E. EMco NOMA Algorithm for EU with MU

Furthermore, when the EU performs NOMA with MU on the NRBs of the HTS in  $L_1$  as shown in Fig. 3 (b) and Fig. 4 (c) in the aforementioned Section II-D and Section II-E, respectively, the signals of EU could decoded first than that of MU due to the delay tolerant of MUs and high EC requirements of EUs. Therefore, the SINR of EUs and MUs on NRBs can be expressed as

$$\gamma_e = \frac{\alpha_e \rho_e |h_e|^2}{\alpha_m \rho_m |h_m|^2 + 1},\tag{36}$$

and

$$\gamma_m = \frac{\alpha_m \rho_m |h_m|^2}{\beta_e \alpha_e \rho_e |h_e|^2 + 1}.$$
(37)

Considering the high EC requirements of EUs, the optimization goal is maximizing  $C(\gamma_e)$  of EU under an appropriate ST threshold for MU. Note that  $T_{m_k}$  approaches  $C(\gamma_{m_k})$  under high SNR, the optimization problem is maximizing  $C(\gamma_e)$ under the an appropriate EC threshold  $C_m^{\text{th}}$  for MU. Similarly, we have the following inequalities

$$\begin{cases} C(\gamma_m) \ge C_m^{\text{th}}, \\ C(\gamma_e) \ge C_e^{\text{th}}, \end{cases}$$
(38)

where  $C_m^{\rm th}$  and  $C_e^{\rm th}$  are the EC requirements of MU and EU,

respectively. By substituting (10) into (38), we have

$$\begin{cases}
\alpha_e \geq \frac{x \cdot \varepsilon_e \Gamma(\mathcal{M}_e)(1+z)}{\rho_e \Gamma(\mathcal{M}_e+1)(1-\beta_e x \cdot z)} = \partial_e^2, \\
\alpha_m \geq \frac{z \cdot \varepsilon_m \Gamma(\mathcal{M}_m)(1+x \cdot \beta_e)}{\rho_m \Gamma(\mathcal{M}_m+1)(1-\beta_e x \cdot x)} = \partial_m,
\end{cases}$$
(39)

where  $x = \left(2^{C_e^{\text{th}}} - 1\right)$ , and  $z = \left(2^{C_m^{\text{th}}} - 1\right)$ . Moreover, the signal of MU is decoded as

Moreover, the signal of MU is decoded after EU in the NRB, and the OP  $F_m(\gamma_m^{\text{th}})$  of MU can be expressed as

$$F_m\left(\gamma_m^{\text{th}}\right) = 1 - \frac{\Gamma\left(\mathcal{M}_m, \frac{\varepsilon_m \gamma_m^{\text{th}}(1+\beta_e \rho_e \alpha_e \frac{\Gamma\left(m_e+1\right)}{\varepsilon_e \Gamma\left(\mathcal{M}_e\right)}\right)}{\rho_m \alpha_m}\right)}{\Gamma\left(\mathcal{M}_m\right)}.$$
 (40)

Therefore, the corresponding optimization problem is established as follows

$$\max C(\gamma_e), \tag{41a}$$

$$s.t.: \partial_m \le \alpha_m \le 1, \tag{41b}$$

$$\partial_e^2 \le \alpha_e \le 1,\tag{41c}$$

$$F_m(\gamma_m^{\rm th}) \le \xi_m. \tag{41d}$$

where (41b) and (41c) indicate the constraints of  $\alpha_m$  and  $\alpha_e$  to satisfy the EC requirements of MU and EU, respectively, and (41d) guarantees the OP of MU  $\xi_m$ .

Similar to the ECco algorithm, we set  $\alpha_e = 1$  due to the high EC requirements of EUs. Then, we adjust  $\alpha_e$  and  $\alpha_c$ to maximize EC of EU under the OP threshold of MU, and propose the EMco algorithm as NOMA 5 in Fig. 3, which is summarized in Algorithm 3.

# F. RBS Algorithm for EU in $L_1$ Layer

In addition, as shown in Fig. 5 in the aforementioned Section II-F, when the EUs perform GB access to the HTS in  $L_1$ , there are three kinds of RBs such as eRBs, NRBs and RRBs for the EUs to perform IEC, EMco NOMA, ECco NOMA algorithms, respectively. We define the statistical EC as the average EC of the UEs at HTS, which is obtained by the HTS after long-term interaction with the UEs. Let  $\bar{C}_1$  denote the statistic EC difference of two EUs and one EU on an eRB with IEC algorithm, and  $\bar{C}_2$  and  $\bar{C}_3$  denote the statistic EC of EU on the NRBs and RRBs, respectively. Thus, in order to achieve the maximum EC for the EUs, we propose the RBS algorithm as follows.

If the  $L_1$  layer HTS knows the above statistic EC  $\bar{C}_1$ ,  $\bar{C}_2$ and  $\bar{C}_3$ , and let  $N_1$ ,  $N_2$  and  $N_3$  denote the number of eRBs, NRBs and RRBs that can be allocated to the EUs, respectively. Then, the HTS broadcasts the RAM4 and RAM5 to grant the *j*-th EU ( $1 \le j \le J$ ) to access an RB as  $EU_j^{w,d}$  to achieve the maximum EC by allocating adaptive number of RBs for EUs, where w, d denote the *w*-th RB in the *d*-th class of RBs, for example,  $EU_5^{2,3}$  means the 5-th EU perform ECco NOMA to the second RRB. The RBS algorithm is summarized in Algorithm 4.

Else, the HTS allocates  $N_1$  EUs with better channel conditions to access the eRBs, and the rest EUs perform random access to the available RBs.

Al	gorithm 3: EMco NOMA Algorithm for MU and EU	<b>Algorithm 4:</b> RBS Algorithm for EU in $L_1$ Layer
co	exist	<b>Input</b> : $N_1, N_2, N_3, \bar{C}_1, \bar{C}_2$ and $\bar{C}_3, EU_i, S_i$ ;
I	<b>nput</b> : $\mathcal{M}_k$ , $\varepsilon_k$ , $\beta_k$ , $\gamma_k^{\text{th}}$ , $\rho_k$ , $h_k$ , $l_k$ , $\xi_m$ , $C_k^{\text{th}}$ , $P_{cur}$ ,	<b>Output</b> : $[EU_1,, EU_J];$
	$P_{max}$ , step length $\Delta_{\alpha_m}$ ;	1 Initialization: $j = 1, w = 1, d = 1, Y_1 = N_1, Y_2 = N_2,$
C	<b>Dutput</b> : $\alpha_m$ and $\alpha_e$ ;	$Y_3 = N_3;$
1 f(	or $P_{cur} \leq P_{max}$ do	<b>2</b> for $j \in [1, N_1]$ and $j \leq J$ , do
2	Calculate $\partial_m$ and $\partial_e^2$ according to Eq. (39);	3 $EU_{i} = EU_{i}^{w,d}; j = j + 1, w = w + 1;$
3	Initialize $\alpha_e = 1$ , and $\alpha_m = \min(1, \partial_m)$ .	4 end
4	Substitute $\alpha_e$ and $\alpha_m$ into Eq. (40) to get $F_m(\gamma_m^{\text{th}})$ .	5 for $j \in [N_1 + 1, 2N_1 + N_2 + N_3]$ and $j \leq J$ do
5	while $\alpha_m < 1$ do	6   if $(\bar{C}_1 = \max(\bar{C}_1, \bar{C}_2, \bar{C}_3) \text{ or } Y_2 = = 0 \text{ or }$
6	Substitute $\alpha_e$ and $\alpha_m$ into Eq. (40) to update	$Y_3 == 0$ and $Y_1 > 0$ then
	$F_m\left(\gamma_m^{\mathrm{th}}\right).$	7 $w = N_1 - Y_1 + 1; d = 1; EU_j = EU_j^{w,d};$
7	if $F_m(\gamma_m^{\text{th}}) > \xi_m$ then	$\begin{array}{c} x \\ y \\ y_1 = Y_1 - 1; \end{array} \qquad $
8	$\alpha_m = \min(1, \alpha_m + \Delta_{\alpha_m});$	$s \mid end$
9	else	9 <b>if</b> $(\bar{C}_2 == \max(\bar{C}_1, \bar{C}_2, \bar{C}_3) \text{ or } Y_1 == 0 \text{ or}$
10	break;	$Y_3 == 0$ and $Y_2 > 0$ and (EU access in $S_{i,1}$ or
11	end	$S_{i,2}$ ) then
12	end	10 $  w = N_2 - Y_2 + 1; d = 2; EU_j = EU_j^{w,d};$
13	while $\alpha_e > \partial_e^2$ do	$Y_2 = Y_2 - 1;$
14	Substitute $\alpha_e$ and $\alpha_m$ into Eq. (40) to update	11 end
	$F_m\left(\gamma_m^{\mathrm{th}}\right)$ .	12 <b>if</b> $(\bar{C}_3 == \max(\bar{C}_1, \bar{C}_2, \bar{C}_3) \text{ or } Y_1 == 0 \text{ or}$
15	if $F_m\left(\widehat{\gamma}_m^{\text{th}}\right) > \xi_m$ then	$Y_2 == 0$ and $Y_3 > 0$ and (EU access in $S_{i,1}$ ) then
16	$\alpha_e = \max(\partial_e^2, \alpha_e - \Delta_{\alpha_e});$	13 $w = N_3 - Y_3 + 1; d = 3; EU_j = EU_j^{w,d};$
17	else	$Y_3 = Y_3 - 1;$
18	break;	14 end
19	end	15 $j = j + 1;$
20	end	16 end
21 ei		17 Return $[EU_1,, EU_J];$
22 R	Return $\alpha_m$ and $\alpha_e$ ;	

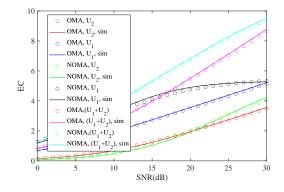


Fig. 6. EC performance of fixed power coefficient NOMA scheme and OMA scheme

# V. SIMULATION AND ANALYSIS

In this section, we present the simulation results to validate the theoretical analysis and show the superiority of our proposed algorithms. The simulation parameters are given in Table III.

# A. Validation of Theoretical Analysis

1) EC: The EC performance of a fixed power coefficient ( $\alpha_1 = 0.2, \alpha_2 = 0.8$ ) NOMA scheme and OMA scheme is shown in Fig. 6. We can observe that the Monte Carlo

TABLE III System Parameters

Parameter	Value
The altitude of HTS in $L_1$ (km)	350
The altitude of HTS in $L_2$ (km)	1200
The number of RBs in each HTS $D$	320
The total number of CUs	200
The total number of MUs	32000
The activation probability of each CU $p_c$	0.2
The activation probability of each MU $p_m$ [7]	0.01
Additive white Gaussian noise (K)	300
Bandwidth of each RB (MHz)	5
Rain attenuation parameters $(\mu, \sigma)$ (dB) [23]	-2.6, 1.6
Maximum HTS beam gain (dBi) [23]	52.1
UE antenna main lobe gain (dBi)	22.1
Imperfect SIC coefficient	$5 \times 10^{-3}$

simulations agree well with our analysis results in Fig. 6, which indicates that our derived expressions Eq. (10), Eq. (11), Eq. (12), Eq. (13) and Eq. (14) can accurately evaluate the EC of our system.

2) *OP*: The OP performance of a NOMA scheme with a fixed power coefficient ( $\alpha = 0.2, \alpha_2 = 0.8$ ) and a fixed SINR threshold ( $\gamma^{\text{th}} = 1$  dB) is shown in Fig. 7. The Monte Carlo simulations validate the accuracy of Eq. (16), Eq. (17) and Eq. (18). Note that the ST expression in Eq. (21) is a multiplicative combination of OP and EC, which can be validated with the above results.

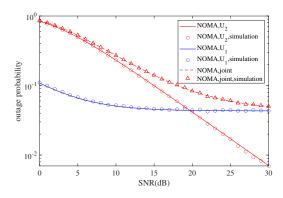


Fig. 7. OP performance of using a fixed power coefficient NOMA scheme

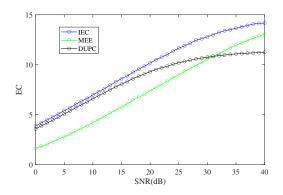


Fig. 8. Comparison of EC performance for EUs.

## B. Comparison of NOMA Algorithms

1) Comparison of EC Performance for EUs: As shown in Fig. 8, the IEC algorithm can achieve better EC performance than other NOMA schemes. For example, the IEC algorithm can save about 4 dB and 9 dB compared with the DUPC and MEE algorithm when reaching the same EC (e.g., EC = 10 bit/s/Hz), respectively.

2) Comparison of OP Performance for CUs: As shown in Fig. 9 (a), the IOP algorithm can achieve the goal of minimizing the OP of each CU, and it can achieve an OP of  $10^{-6}$  per CU at SNR about 39 dB. Meanwhile, as shown in Fig. 9 (b), the IOP algorithm can achieve much better joint OP for each CU NOMA group than the MEE NOMA algorithm, and can save 7 dB than the DUPC algorithm when reaching the same OP performance at higher SNR (> 25 dB).

3) Comparison of ST Performance for MUs: As shown in Fig. 10, at higher SNR (> 6dB), the IST algorithm can achieve better ST performance than other NOMA schemes, and save 4 dB and 8 dB compared with MEE and DUPC algorithms when reaching the same ST performance (e.g., ST = 10 bit/s/Hz), respectively.

4) Comparison of EC performance for EU and CU coexistence: As shown in Fig. 11 that although the ECco NOMA algorithm has lower EC of EU due to the OP requirements of CU, the proposed ECco NOMA algorithm can approach higher sum EC performance than that of MEE algorithm before the high SNR region ( $\leq$  30 dB), and can obtain better EC performance than the DUPC algorithm.

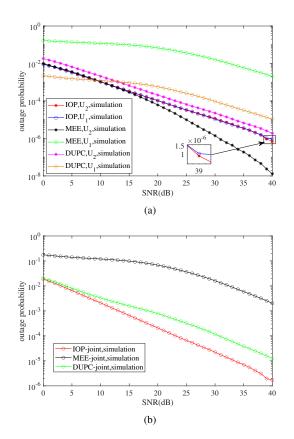


Fig. 9. Comparison of OP performance for (a)  $U_1$  and  $U_2$  separately and (b) CU NOMA group.

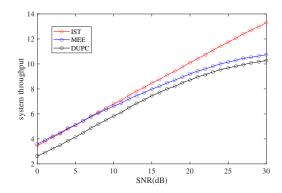


Fig. 10. Comparison of ST performance for MU group.

5) Comparison of EC performance for EU and MU coexistence: As shown in Fig. 12, the proposed EMco NOMA algorithm can save about 10 dB and 18 dB compared with MEE and DUPC algorithms when reaching the same EC at higher SNR (> 22dB), respectively.

## C. Comparison of EC performance of RBS Algorithm

As shown in Fig. 13, when fixing the SNR of each EU as 30dB, the EC gain of RBS algorithm compared with the random access (RA) algorithm in  $S_{i,1}$  and  $S_{i,2}$  subframes, and the average EC for each EU with RBS algorithm is better than the RA algorithm with different numbers of access EUs. Specifically, when J = 60, the RBS algorithm can obtain

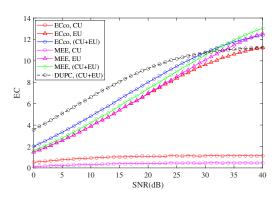


Fig. 11. Comparison of EC performance for CU with EU performing joint NOMA.

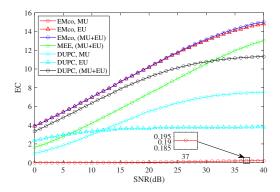


Fig. 12. Comparison of EC performance for MU with EU performing joint NOMA.

about 4.2% EC gain in  $S_{i,1}$  compared with the RA algorithm. In addition, when J = 200, the EC gain of RBS algorithm compared with RA algorithm in  $S_{i,1}$  and  $S_{i,2}$  is about 16.4% and 59.9%, respectively. Further, when J = 270, the EC gain of RBS algorithm compared with RA algorithm in  $S_{i,1}$  and  $S_{i,2}$  is about 1% and 11.5%, respectively.

# VI. CONCLUSION

In this paper, we have proposed the MSCH NOMA scheme to guarantee the KPI requirements of multi-type UEs coexistence in the dual-layer LEO HTS constellation. Specifically, we first proposed a handover transmission scheme for EUs in a dual-layer LEO HTS constellation, then we proposed the SGF random access protocols for CUs, MUs and EUs performing coexist uplink transmission, and further proposed the RAM generator to control transmissions of the UEs. Moreover, we have derived the closed-form expressions of KPIs (i.e., OP, EC and ST) to measure the performance of different types of UEs, and utilized them to design the NOMA algorithms, where the IEC and IST NOMA algorithms can maximum the EC of EUs and ST of MUs under an appropriate OP thresholds, respectively, and the IOP NOMA algorithm can minimize OP of each CUs, and the ECco and EMco NOMA algorithms both can maximize the EC of EUs under an appropriate OP threshold for CUs or MUs, respectively. In addition, we have proposed an RBS algorithm to further improve the EC of EUs. Finally, the accuracy of our derived expressions has been verified by Monte Carlo simulations, and extensive simulation

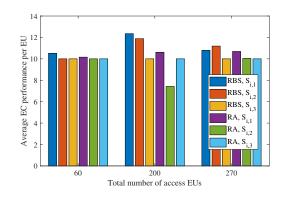


Fig. 13. Comparison of EC performance for EU scheduling strategy.

results demonstrate that the proposed NOMA algorithms have better OP, EC and ST performance than the MEE-NOMA and DUPC-NOMA algorithms.

# APPENDIX A Derivations of Eq. (11) to Eq. (14)

Since the first order moment expression of  $\gamma_{k,b}$  can be calculated by:

$$E[\gamma_{k,b}] = \int_0^\infty [1 - F_{k,b}(x)] dx.$$
 (42)

By substituting Eq. (16) and Eq. (17) into Eq. (42), and with the help of [37, Eq.(6.455.1)], we can get the first-moment expression of  $\gamma_{1,b}$  and  $\gamma_{2,b}$  as Eq. (11) and Eq. (13), respectively.

In addition, the second order moment expression of  $\gamma_{k,b}$  can be calculated by:

$$E\left[\left(\gamma_{2,b}\right)^{2}\right] = 2\int_{0}^{\infty} x\left[1 - F_{2,b}(x)\right] dx.$$
 (43)

Then, we can get the second-moment expression of  $\gamma_{1,b}$  and  $\gamma_{2,b}$  as Eq. (12) and Eq. (14), respectively, by substituting Eq. (16) and Eq. (17) into Eq. (47) and via [37, Eq.(6.455.1)].

# Appendix B

# DERIVATION OF EQ. (16) AND EQ. (17)

By substituting Eq. (7) into Eq. (15), and with the help of [37, Eq.(3.351.2)], we can derive the OP of  $U_1$  at  $H_b$  as follows:

$$\begin{aligned} F_{\gamma_{1,b}}(\gamma_{1,b}^{\mathrm{th}}) &= \Pr(\gamma_{1,b} < \gamma_{1,b}^{\mathrm{th}}) \\ &= \Pr(\frac{\alpha_{1,b}\rho_{1,b}|h_{1,b}|^2}{\alpha_{2,b}\rho_{2,b}|h_{2,b}|^2 + 1} < \gamma_{1,b}^{\mathrm{th}}), \\ &= \Pr(|h_{1,b}|^2 < \frac{\gamma_{1,b}^{\mathrm{th}}(\alpha_{2,b}\rho_{2,b}|h_{2,b}|^2 + 1)}{\alpha_{1,b}\rho_{1,b}}), \\ &= \int_0^{\frac{\gamma_{1,b}^{\mathrm{th}}(\alpha_{2,b}\rho_{2,b}|h_{2,b}|^2 + 1)}{\alpha_{1,b}\rho_{1,b}}} f_{|h_{1,b}|^2}(y) dy \qquad (44) \\ &= 1 - \int_{\frac{\gamma_{1,b}^{\mathrm{th}}(\alpha_{2,b}\rho_{2,b}|h_{2,b}|^2 + 1)}{\alpha_{1,b}\rho_{1,b}}} f_{|h_{1,b}|^2}(y) dy, \\ &\stackrel{\underline{A}}{=} 1 - \frac{\Gamma\left(M_{1,b}, \frac{\varepsilon_{1,b}\gamma_{1,b}^{\mathrm{th}}(1 + \rho_{2,b}\alpha_{2,b}|h_{2,b}|^2)}{\rho_{1,b}\alpha_{1,b}}\right)}{\Gamma(M_{1,b})} \end{aligned}$$

where Eq. A is derived with the help of [37, Eq.(3.351.2)].

Similarly, by substituting Eq. (4) into Eq. (5), and with the help of [37, Eq.(3.351.2)], we can derive the OP of  $U_2$  at  $H_b$ as

$$F_{2,b}(\gamma_{2,b}^{\text{th}}) = 1 - \frac{\Gamma\left(M_{2,b}, \frac{\varepsilon_{2,b}\gamma_{2,b}^{th}(1+\beta_{1,b}\rho_{1,b}\alpha_{1,b}|h_{1,b}|^2)}{\rho_{2,b}\alpha_{2,b}}\right)}{\Gamma(M_{2,b})}.$$
(45)

Since  $|h_{k,b}|^2$  of each  $U_k$  at  $H_b$  obeys the log-normal distribution, we utilized the expected value of  $|h_{k,b}|^2$ ,  $|h_{k,b}|^2_{mean}$ to simplify the calculation.

With the help of [37, Eq.(3.381.11), we can obtain the  $|h_{k,b}|_{mean}^2$  as

$$\begin{aligned} |h_{k,b}|^{2}_{mean} &= \int_{-\infty}^{\infty} x \cdot \frac{\varepsilon_{k,b}^{\mathcal{M}_{k,b}}}{\Gamma\left(\mathcal{M}_{k,b}\right)} x^{\mathcal{M}_{k,b}-1} \exp\left(-\varepsilon_{k,b} \cdot x\right) dx \\ &= \frac{\varepsilon_{k,b}^{\mathcal{M}_{k,b}}}{\Gamma\left(\mathcal{M}_{k,b}\right)} \cdot \int_{-\infty}^{\infty} x^{\mathcal{M}_{k,b}} \exp\left(-\varepsilon_{k,b} x\right) dx \\ &= \frac{\Gamma\left(\mathcal{M}_{k,b}+1\right)}{\varepsilon_{k,b} \cdot \Gamma\left(\mathcal{M}_{k,b}\right)}. \end{aligned}$$
(46)

By substituting Eq. (46) into Eq. (44) and Eq. (45), we can get the closed-form expression of OP for  $U_1$  and  $U_2$  at  $H_b$  as Eq. (16) and Eq. (17), respectively.

# APPENDIX C

The relationship of 
$$\alpha_{e_1,b}$$
 and  $\alpha_{e_2,b}$  with  $C(\gamma_{e_1,b})$ 

Since  $\frac{\rho_{1,b}\alpha_1\Gamma(\mathcal{M}_{1,b}+1)}{(1+\rho_{2,b}\cdot\alpha_2\frac{\Gamma(\mathcal{M}_{2,b}+1)}{\varepsilon_{2,b}\Gamma(\mathcal{M}_{2,b})})\varepsilon_{1,b}\cdot\Gamma(\mathcal{M}_{1,b})}$  is much larger than 1 at higher SNR  $\rho_{1,b}$  of  $U_1$  at  $H_b$ , the EC  $C(\gamma_{1,b})$  of  $U_k$  at

 $H_b$  can be approximated as

$$C(\gamma_{1,b}) = \log_{2}(e) \cdot \left[1 + \frac{\rho_{1,b}\alpha_{1}\Gamma\left(\mathcal{M}_{1,b}+1\right)}{\left(1 + \rho_{2,b}\alpha_{2}\frac{\Gamma(\mathcal{M}_{2,b}+1)}{\varepsilon_{2,b}\cdot\Gamma(\mathcal{M}_{2,b})}\right)\varepsilon_{1,b}\Gamma\left(\mathcal{M}_{1,b}\right)}\right] - \log_{2}(e) \cdot \frac{\frac{\Gamma(\mathcal{M}_{1,b})}{\Gamma(\mathcal{M}_{1,b}+1)} - 1}{2}.$$
(47)

$$\frac{\Gamma(\mathcal{M}_{1,b})}{\Gamma(\mathcal{M}_{1,b}+1)} - 1 \qquad (47)$$

Note that  $-\frac{\Gamma(2^{(1)}, \beta+1)}{2}$  is a constant, we can straightforwardly derive that  $\alpha_{1,b}$  is strictly positive with  $C(\gamma_{1,b})$  and  $\alpha_{2,b}$  is negative with  $C(\gamma_{1,b})$ .

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